Exoplanets Doppler method

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# Indirect Methods: gravitational perturbation of the stellar motion

- The star and the planet orbit around their common barycenter
  - The stellar motion, induced by the gravitational perturbation of the planet, is called "reflex motion"



Exercise:

show that the Jupiter-Sun barycenter lies outside the volume of the Sun, by 7% of the Sun's radius

## Indirect Methods:

## gravitational perturbation of the stellar motion

$$a_* = a \, rac{M_p}{M_*}$$

The reflex motion of the star is proportional to  $M_p/M_*$ This introduces an observational bias

that favours the detection of massive planets around low-mass stars

Indirect methods based on the perturbation of the stellar motion: Radial Velocity (or Doppler) Timing Astrometric

# Doppler method

- Spectroscopic measurement
  - Based on the measurement of the radial velocity of the stellar reflex motion at different epochs
    - The stellar radial velocity contains a variable term,  $V_* \sin i$ , due to the projection of the reflex motion along the line of sight
    - Thanks to the Doppler effect, the variable term  $V_*$  sin induces a periodic shift of the photospheric lines of the stellar spectrum
- Requires high resolution spectroscopy
  - e.g., Echelle spectroscopy



$$\Delta \lambda = \lambda_{\rm obs} - \lambda_{\rm em}$$

$$v_r \simeq \left(rac{\Delta\lambda}{\lambda_{
m em}}
ight)c$$

### Masurement of the stellar radial velocity

- Based on the measurement of the centroid of stellar absorption lines
- The central position of the absorption line,  $\lambda_c$ , can be measured with linefitting methods
- For unblended, unsaturated lines, a Gaussian fit generally provides an accurate determination of the centroid
- The centroid  $\lambda_c$  is compared with the laboratory wavelength of the electronic transition responsible for the absorption,  $\lambda_o$
- In this way we calculate the radial velocity: in the non-relativistic case, the radial velocity is

$$V_{\rm r} = c \ (\lambda_{\rm c} - \lambda_{\rm o}) / \lambda_{\rm o}$$

## Radial velocity curves

- Obtained by plotting the stellar radial velocity as a function of time
- If a periodicity is determined, data taken at different epochs are rescaled as a function of orbital phase



Radial velocity curve of 51 Peg b,

the first exoplanet detected with the Doppler method (Mayor et al. 1995)

## Radial velocity curves

- For circular orbits with  $M_p \ll M_*$  the Keplerian radial velocity curves are sinusoidal
- In general, radial velocity curves can have different shape, depending on the eccentricity, e, and the argument of the pericenter,  $\omega$



- Parameters that can be derived from the radial velocity curve
- Semi-amplitude, *K*, and period, *P*

The amplitude corresponds to the variation of  $V_* \sin i$  during one orbital period Radial Velocity Measurements using Doppler



– The semi-amplitude is given by

$$K = \left(\frac{2\pi G}{P}\right)^{1/3} \frac{M_p \sin i}{(M_\star + M_p)^{2/3}} \frac{1}{(1 - e^2)^{1/2}}$$

The above expression for *K* can be used to estimate the expected effect for the Solar System planets

	Radial V				
Planet	${f M}_p \ ({f M}_J)$	R (AU)	P (years)	$\Theta_{\star}$ at 10 pc (mas)	$(ms^{-1})$
Mercury Venus Earth Mars Jupiter Saturn Uranus Neptune Pluto	1.74E-4 2.56E-3 3.15E-3 3.38E-4 1.0 0.299 0.046 0.054 6.3E-6	$\begin{array}{c} 0.387\\ 0.723\\ 1.000\\ 1.524\\ 5.203\\ 9.54\\ 19.18\\ 30.06\\ 39.44 \end{array}$	$\begin{array}{c} 0.241 \\ 0.615 \\ 1.000 \\ 1.881 \\ 11.86 \\ 29.46 \\ 84.01 \\ 164.8 \\ 247.7 \end{array}$	6.4E-6 1.8E-4 3.0E-4 4.9E-5 0.497 0.273 0.084 0.156 2.4E-5	0.008 0.086 0.089 0.008 12.4 2.75 0.297 0.281 3E-5

## Doppler method Selection effects

For a given stellar mass, the amplitude of the reflex motion scales as  $M_p P^{-1/3}$ Easier to detect massive planets with short orbital period (i.e., small semimajor axis)

For a given planetary mass, the amplitude of the reflex motion scales as  $M_*^{-2/3}$ Easier to detect <u>planets around low-mass stars</u> (e.g. M type stars) Low-mass stars are intrinsically fainter, but more numerous, than stars of higher mass

The amplitude of the reflex motion is larger when the line of sight is aligned with the orbital plane (sin  $i \approx 1$ )

If orbits are oriented at random, this selection effect does not introduce a bias on the physical properties of the planetary systems

- Derivation of orbital and planetary parameters with the Doppler method
  - The radial velocity curves provides the period, P, from which the semimajor axis a is inferred using the third Kepler's law
  - The mass of the star is derived from a spectroscopic study combined with a model of stellar structure
  - By fitting the radial velocity curve one can obtain the eccentricity, e, and the argument of the pericenter,  $\omega$
  - In this way, from the semiamplitude K one can infer a lower limit on the planet mass

$$M_p \sin i = K \left(\frac{P}{2\pi G}\right)^{1/3} (M_\star + M_p)^{2/3} (1 - e^2)^{1/2}$$

- The orbital inclination
  - Systems with high inclination give a higher radial radial velocity signal and, in this sense, are more likely to be detected
  - <u>Statistically</u>, the correction term sin *i* is not very large
  - The statistical probability that the orbital inclination is within an arbitrary range  $(i_1, i_2)$  is (Fischer et al. 2014)

$$\mathcal{P} = |\cos(i_2) - \cos(i_1)|$$

- There is roughly an 87% probability that random orbital inclinations are between 30 and 90, or equivalently, an 87% probability that the true mass is within a factor of 2 of the minimum mass  $M_p \sin i$
- In any case, a safe determination of the mass requires an independent measurement of the orbital inclination, i

### Doppler method Cross correlation spectroscopy

Information on the instantaneous Doppler shift is contained in the many thousands of absorption lines present in the high-resolution optical spectra of solar-type stars

This information can be concentrated into a few parameters by crosscorrelation with a template of the expected stellar spectrum In practice, one has to determine the value of  $\epsilon$  minimizing

$$C(\epsilon) = \int_{-\infty}^{+\infty} S(v) M(v - \epsilon) dv$$

where S is the spectrum, M is the mask (i.e. a numerical template), both expressed in velocity space v

Thanks to the use of thousands of absorption lines, the cross correlation is efficient even at low signal-to-noise ratio

### Doppler method Cross correlation spectroscopy

Example cross-correlation function for a K0 III star with S/N ~ 1. Observations at R=40000 in 10 echelle orders, each covering ~ 4 nm. About 1000 lines match the template. The resulting cross-correlation function is shown at the bottom.

(Queloz 1995)



### Doppler method

### • Technological requirements

Extremely stable spectrograph

- Long term stability in temperature (possibly years)
- The spectrograph is closed in a separate room/container, fed by optical fibres

High accuracy of wavelength calibration

- Control of the optical paths of the stellar and wavelength calibration spectra
- Thorium-argon calibration

Classic observations

Laser frequency combs

Cover the entire wavelength range of interest with a series of calibration lines of uniform spacing and intensity and accurately known wavelengths determined by fundamental physics

### • Mass limit of detectability

Minimum mass limit for a 50% detection threshold as a function of the number of observations, N, and the combined error,  $\sigma$ , for  $M_*=1$  $M_{sun}$ 

- In addition to the measurement error, the "stellar jitter" (activity in the stellar atmosphere and stellar oscillations) contributes to the combined error  $\sigma$
- With increasing measurement accuracy, stellar jitter becomes the most severe limit of application of the method



# Doppler method: examples of spectrographs

- HARPS
  - High Accuracy Radial velocity Planet Searcher
  - Telescope: ESO 3.6m La Silla (Cile)
    - http://www.eso.org/sci/facilities/lasilla/instruments/harps/
  - Has played a pioneering role, and is still effective, in the search for extrasolar planets
  - Estremely stable, with current limits of radial velocity accuracy ~40 cm/s for planets orbiting relatively bright stars (V~12)
- HARPS-north
  - Based on the HARPS spectrograph, installed in 2012 at the Italian national telescope TNG (3.5m, La Palma, Spain)
  - Extends the capabilities of HARPS to the northern hemisphere

### • ESPRESSO

- Echelle SPectrograph for Rocky Exoplanet and Stable Spectroscopic Observations
  - http://www.eso.org/sci/facilities/develop/instruments/espresso.html
- Extremely stable, recently installed at the combined focus of the ESO VLT (8m x 4)
  - Radial velocity accuracy: < 10 cm/s
  - Fainter stars than observable with HARPS
- Detection of terrestrial-type planets at ~1 AU around solar-type stars



### Doppler method

- Very effective
  - Between 1995 and 2012 most exoplanets have been discovered with the Doppler method
  - Currently (January 2018) detected 743 planets in 553 planetary systems



#### Doppler method comparison with other methods

Mass - Period Distribution





### Detection of <u>multiple planetary systems</u> with the Doppler method

- The total radial velocity signal due an orbiting system of  $n_p$  planets is assumed to result from the independent reflex motions due to each planet separately
- Procedure:
  - Make a Keplerian fit of the most intense signal of the radial velocity curve
  - Subract the Keplerian fit to the experimental data and search for more periodic signals in the residuals
  - If the periodogram (Fourier transform) of the residuals shows a peak above the noise level, a further Keplerian fit is performed
- The procedure can be iterated if the periodogram of the residuals shows additional significant peaks

#### Example: Two-planet system orbiting HD215497 (Lo Curto et al. 2010)



#### Example: Two-planet system orbiting HD215497 (Lo Curto et al. 2010)

Keplerian fit of the residuals, using the orbital parameters determined from the previous step

#### Final results



Parameter	HD 215497b	HD 215497c	
P [days]	$3.93404 \pm 0.00066$	$567.94 \pm 2.70$	
T [JD-2400000]	$54858.95\pm0.37$	$55003.48\pm5.15$	
е	$0.16 \pm 0.09$	$0.49 \pm 0.04$	
$\omega$ [deg]	$96 \pm 34$	$45 \pm 4$	
$K [{\rm m \ s^{-1}}]$	$2.98 \pm 0.34$	$10.10 \pm 0.65$	
$V [{\rm km \ s^{-1}}]$	$49.3107 \pm 0.0006$		
$m\sin i \left[M_{\rm Jup}\right]$	0.02	0.33	
$m \sin i [M_{\text{Earth}}]$	6.6	104.3	
a [AU]	0.047	1.282	
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## Doppler method future projects

- CODEX
  - Instrument concept for the European ELT (Extremely Large Telescope)
  - It aims to detect the expansion of the Universe directly, by measuring the Doppler shift of high-redshift quasar Ly- $\alpha$  absorption lines as a function of time
  - The experiment targets a Doppler accuracy of ~0.02 m/s mantained over several <u>decades</u>
  - The design has developed from HARPS and will incorporate all the state-of-the-art technology (e.g. laser comb, etc.)
  - CODEX will have direct application to exoplanet studies
  - Stellar jitter would definitely become the major limitation