Observational constraints for models of planetary formation

Planets and Astrobiology (2019-2021) G. Vladilo and S. Ivanovski Observational constraints of Solar System formation

Dynamical constraints

- Orbital motions of the planets
 - Most orbits are coplanar with the Sun equator
 - Most orbits are prograde with respect to solar rotation
- These characteristics suggest a common origin of the Sun and the planets through a process that has preserved the angular momentum
 - Consistent with an origin in a "solar nebula" with a disk shape

Hypothesis already advanced, in schematic form, by Laplace As a result of the contraction of the nebula, a disk is formed which provides the material for the planetary formation

The angular momentum of the Solar System $L = r \times mv$

• Rotational angular momentum

$$\begin{array}{ll} L^{(rot)}{}_{Sole} &= 1,6\!\cdot\!10^{40}~(kg\!\cdot\!m^2)/s \\ L^{(rot)}{}_{Giove} &= 4,5\!\cdot\!10^{38}~(kg\!\cdot\!m^2)/s \\ L^{(rot)}{}_{Saturno} &= 7,7\!\cdot\!10^{37}~(kg\!\cdot\!m^2)/s \end{array}$$

• Orbital angular momentum of the planets

$$L^{(orb)}_{Giove} = 1,9 \cdot 10^{43} (kg \cdot m^2)/s$$

 $L^{(orb)}_{Saturno} = 7,9 \cdot 10^{42} (kg \cdot m^2)/s$

• Most angular momentum of the Solar System is concentrated in the orbital angular momentum of giant planets

The problem of the angular momentum

- In the nebular hypothesis, one would expect that most of the angular momentum was accumulated in the Sun
- The fact that 98% of the angular momentum lies in the orbital angular momentum of giant planets poses, in principle, a problem for the simple scenario of a common origin from the Solar Nebula
- We must invoke that the Sun has lost angular momentum Possibly:
 - In the protostellar phase, when part of the accreted momentum was used to energize bipolar outflows/jets
 - During the main-sequence evolution: part of the rotational energy is transformed in magnetic fields and solar wind through different types of mechanisms (e.g. the dynamo mechanism)

Constraints on the solar nebula: Density gradient and minimum mass

- Radial distribution of the mass in the solar nebula
 - Approximate estimate based on the following hypothesis:

Each planet, at the epoch of its formation, has accreted all the mass available in its region of influence in the nebula

Rocky planets have lost their volatile components: the mass of the nebula in their region of influence should be scaled from the mass measured in the refractory component

THE DISTRIBUTION OF MASS IN THE PLANETARY SYSTEM AND SOLAR NEBULA

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(Received 19 February, 1977)

Constraints on the solar nebula: Density gradient and minimum mass

• Radial distribution of the nebular mass

 The density profile obtained with the above hypothesis provides a minimum surface density of the solar nebula

The profile has a negative density gradient, in agreement with the expectation that the nebula was thicker in the central regions

By integrating the profile one obtains the "minimum mass solar nebula (MMSN): 0.01 e 0.07 M_{\odot}

- The profile shows anomalies, possibly related to the loss of mass in the asteroid belt
- The MMSN is important for historical reasons
 - Nowaday, we know that it is oversimplified since it does not take into account the possibility of planet migration



Radial gradients of refractory and volatile elements

Volatile and refractory elements are distinguished according to their <u>condensation temperature</u> T_{cond}

Temperature at which an element condenses out of a cooling gas of given composition and pressure Each element can condense in different chemical compounds

Volatiles: $T_{\rm cond} < 10^3 \, {\rm K}$

Refractories: $T_{\rm cond} \gtrsim 10^3 \, {\rm K}$

Substance	Formula	Temperature of condensation ^a (K)
ionic substances		
corundum	Al_2O_3	1758
perovskite	CaTiO ₃	1647
spinel	$MgAl_2O_4$	1513
nickel-iron metal	Ni, Fe	1471
pyroxene (diopside)	$CaMgSi_2O_6$	1450
olivine (forsterite)	Mg_2SiO_4	1444
alkali feldspars	(Na,K)AlSi ₃ O ₈	<1000
troilite	FeS	700
hydrated minerals ^{b}	(variable)	550-330
molecular substances		
water	H_2O (as an ice)	180
ammonia	NH ₃ .H ₂ O (ice)	120
methane	$CH_4.6H_2O$ (ice)	70
nitrogen	$N_2.6H_2O$ (ice)	70

^{*a*} The temperatures of condensation given are those that would occur if the pressure in the nebula had been about 10^{-3} bar (10^2 Pa). At lower pressures, the condensation temperatures would have been reduced slightly.

^{*b*} Hydrated minerals are chiefly silicates with OH or H_2O in their formulae.

Radial gradients of refractory/volatile components in the Solar System

- Inner solar system: the bulk ingredients of rocky planets are refractories – Silicate mantles and iron cores: $T_{cond} > 10^3$ K
- Outer solar system: the bulk ingredients of giant planets are volatiles

– Gasesous and icy volatiles and ices: $T_{\rm cond} \sim 10^2 \,\rm K$

- Similar differences between the inner and outer solar system are found in minor bodies:
 - Asteroids, closer to the Sun, are in large part rocky
 - Comets, at larger distances, are mostly icy

Radial gradients of refractory and volatiles elements: implications for the formations of the Solar System

- The radial gradient of the refractories and volatiles suggests the existence of a temperature gradient in the solar nebula, consistent with what expected from the radiative heating of the nebula by the protosun
- The distance at which (icy) volatiles start to predominate with respect to refractories is called the "snow line" (or "ice line")
 - Simplest definition of "snow line":

Distance from the Sun at which a body heated by solar radiation and cooled by black body emission attains an equilibrium temperature that allows ices to be formed (H_2O , NH_3 , CH_4)

 The real calculation of the ice line is more complicated since one must also take into account the radiative transfer through the protoplanetary disk and other physical processes at the level of microscopic solids

The ice line

Example: calculation of the ice line given the solar luminosity, L_{\odot} , the condensation temperature of ice, T_{ice} , and the ice albedo, A

General equations: $\sigma T^{4}_{eff} = \frac{1}{4} S (1-A)$ $S = L /(4 \pi d_{ice}^{2})$

$$d_{
m ice} \simeq rac{1}{4\,T_{
m ice}^2} \sqrt{rac{L_\odot\,(1-A)}{\pi\sigma}}$$

Solutions for the solar system:

$$d_{\rm ice}[{\rm AU}] \simeq \left(\frac{272}{T_{\rm ice}[{\rm K}]}\right)^2 \sqrt{(1-A)}$$

Gives $d_{ice} \sim 2.3$ AU for $T_{ice}=150$ K and A=0.5

Processes leading to the radial gradient of volatiles/refractories

• Condensation of solids *in situ* in the nebula

the refractory component can condense at all distances from the protosun, while the volatile components can condense only beyond the ice line

 Acquisition of solids (dust grains) previously formed the interstellar medium the refractory components acquired from the interstellar medium can approach the vicinity of the sun, while the volatile component would sublimate the icy component acquired from the interstellar medium can persist only far from the protosun

Time scales of formation of the inner Solar System Based on radiodating techniques



Encyclopedia of the Solar System

Observational constraints on planetary formation obtained from studies of exoplanet systems

• Hot Jupiters

The presence of gaseous giants in the proximity of the star requires mechanisms of radial migration of giant planets

- Peak in the distribution of orbital periods at *P* ~ 3 days
 Requires mechanisms capable of stopping the migration towards the star
 Cases may exist in which the migrating planet is not stopped and merges with the central star
- Dispersion of the values of orbital eccentricities and inclinations Requires mechanisms of gravitational scattering of planetary orbits

Observational constraints on planetary formation obtained from studies of exoplanet systems

• Diversity of possible types of planets

Requires models of planetary formation capable of producing, "super-Earths", "ocean planets, "inflated Jupiters"

Example: EPIC 229426032 b has a mass of about 1.36 Jupiter masses and is approximately 63 percent larger than our solar system's biggest planet. These values indicate a very low density of EPIC 229426032 b—about 0.38 g/cm³, which suggests that this planet is highly inflated.

• Occurrence rate versus metallicity of the host star

If interpreted as a primordial effect, rather than self-enrichment, requires exploring the dependence on metallicity of the processes involved in planetary formation

The dust-to-gas ratio is expected to scale with the level of metallicity

The accretion of solids in the protoplanetary disk scales with the local dust-to-gas ratio, which may be enhanced with respect to the interstellar value ~0.01

Appendix: Radioactive dating

Isochron methodology

We call P(t) and D(t) the time-dependent abundance of the parent and daughter isotopes. The time-dependence of the parent isotope is

$$P(t) = P(0) e^{-kt}$$
(1)

where k is the decay constant (the half-time of decay is $\tau = \ln 2/k$). The sum of the parent and daughter isotopes is constant with time:

$$D(t) + P(t) = D(0) + P(0)$$
(2)

If there is a stable isotope D' of the daugther element D, and we presume that D' is constant throughout the process, then

$$\frac{D(t) + P(t)}{D'} = \frac{D(0) + P(0)}{D'}$$
(3)

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By replacing (1) in the above expression we obtain

$$\frac{D(t)}{D'} = \frac{P(t)}{D'} \left[e^{kt} - 1 \right] + \frac{D(0)}{D'}$$
(4)

If we call y = D(t)/D' and x = P(t), we have

$$y = x \left[e^{kt} - 1 \right] + y(0) \tag{5}$$

By plotting y versus x the slope will be $dy/dx = e^{kt} - 1$ and the age

$$t = \frac{1}{k} \ln \left[1 + \frac{dy}{dx} \right] \tag{6}$$

In this way, if there are samples of the same age, we will obtain an isochrone from which the age can be derived.

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Isochron methodology



⁸⁶Sr is of non-radiogenic origin and can be used as a reference concentration to imply the original concentration of ⁸⁷Sr.