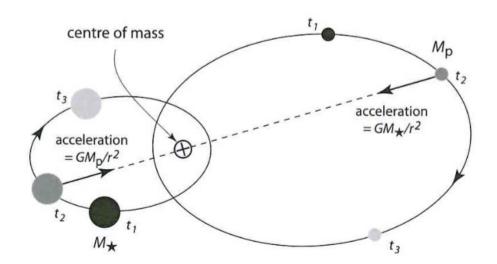
# Exoplanets Radial-velocity method

Planets and Astrobiology (2020-2021) G. Vladilo

# Indirect Methods: gravitational perturbation of the stellar motion

- The star and the planet orbit around their common barycenter
  - The stellar motion, induced by the gravitational perturbation of the planet, is called "reflex motion"



#### Exercise:

show that the Jupiter-Sun barycenter lies outside the volume of the Sun, by 7% of the Sun's radius

# Indirect Methods: gravitational perturbation of the stellar motion

$$a_* = a\,rac{M_p}{M_*}$$

The reflex motion of the star is proportional to  $M_p/M_*$ 

This introduces an observational bias that favours the detection of massive planets around low-mass stars

Indirect methods based on the perturbation of the stellar motion:

Radial Velocity (or Doppler)

Timing

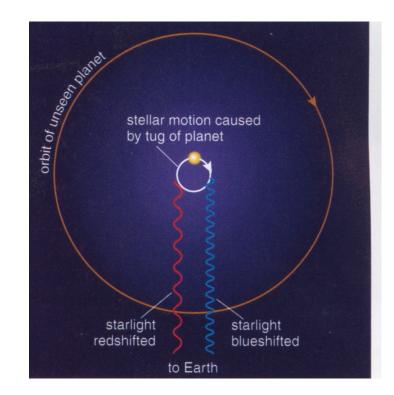
Astrometric

# Doppler method

- Spectroscopic measurement
  - Based on the measurement of the radial velocity of the stellar reflex motion at different epochs
    - The stellar radial velocity contains a variable term,  $V_* \sin i$ , due to the projection of the reflex motion along the line of sight

Thanks to the Doppler effect, the variable term  $V_* \sin i$  induces a periodic shift of the photospheric lines of the stellar spectrum

- Requires high resolution spectroscopy
  - e.g., Echelle spectroscopy



$$\Delta \lambda = \lambda_{\rm obs} - \lambda_{\rm em}$$

$$v_r \simeq \left(\frac{\Delta \lambda}{\lambda_{
m em}}\right) c$$

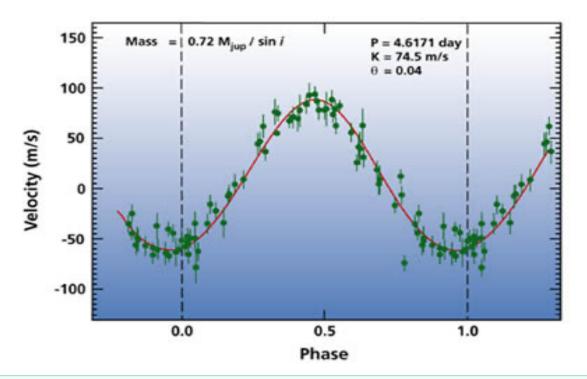
### Masurement of the stellar radial velocity

- Based on the measurement of the centroid of stellar absorption lines
- The central position of the absorption line,  $\lambda_c$ , can be measured with line-fitting methods
- For unblended, unsaturated lines, a Gaussian fit generally provides an accurate determination of the centroid
- The centroid  $\lambda_c$  is compared with the laboratory wavelength of the electronic transition responsible for the absorption,  $\lambda_o$
- In this way we calculate the radial velocity: in the non-relativistic case, the radial velocity is

$$V_{\rm r} = c (\lambda_{\rm c} - \lambda_{\rm o}) / \lambda_{\rm o}$$

# Radial velocity curves

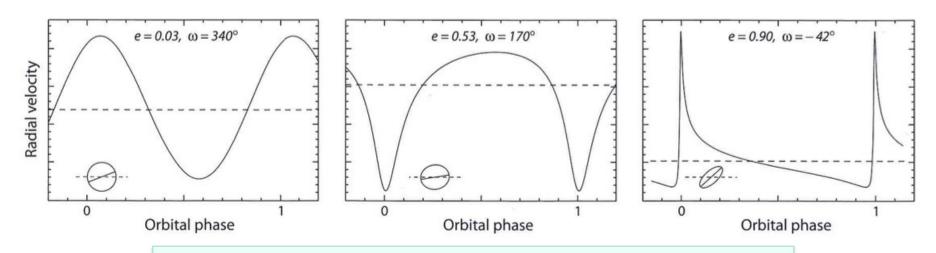
- Obtained by plotting the stellar radial velocity as a function of time
- If a periodicity is found, data taken at different epochs are rescaled as a function of orbital phase



Radial velocity curve of 51 Peg b, the first exoplanet detected with the Doppler method (Mayor et al. 1995)

# Radial velocity curves

- For circular orbits with  $M_p \ll M_*$  the Keplerian radial velocity curves are sinusoidal
- In general, radial velocity curves can have different shape, depending on the eccentricity, e, and the argument of the pericenter,  $\omega$



Examples of radial velocity curves

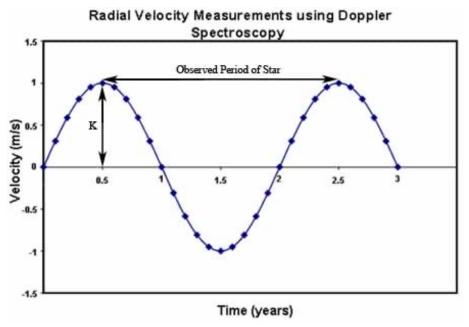
left: HD73256 - center: HD142022 - right: HD4114

dashed lines: radial velocity of the barycenter

- Parameters that can be derived from the radial velocity curve
- Semi-amplitude, K, and period, P

The semi-amplitude is the variation of  $V_* \sin i$  during one half

of the orbital period



The semi-amplitude is given by

$$K = \left(\frac{2\pi G}{P}\right)^{1/3} \frac{M_p \sin i}{(M_{\star} + M_p)^{2/3}} \frac{1}{(1 - e^2)^{1/2}}$$

From the above expression for *K* one can estimate the impact on the solar motion induced by the planets of the Solar System

W. D. COCHRAN AND A. P. HATZES

Table I Radial Velocity Signals of the Planets

					-K
Planet	$egin{array}{c} \mathrm{M}_p \ \mathrm{(M}_J) \end{array}$	R (AU)	P (years)	Θ <sub>*</sub> at 10 pc (mas)	$(ms^{-1})$
Mercury	1.74E-4	0.387	0.241	6.4E-6	0.008
Venus	2.56E-3	0.723	0.615	1.8E-4	0.086
Earth	3.15E-3	1.000	1.000	3.0E-4	0.089
Mars	3.38E-4	1.524	1.881	4.9E-5	0.008
Jupiter	1.0	5.203	11.86	0.497	12.4
Saturn	0.299	9.54	29.46	0.273	2.75
Uranus	0.046	19.18	84.01	0.084	0.297
Neptune	0.054	30.06	164.8	0.156	0.281
Pluto	6.3E-6	39.44	247.7	2.4E-5	3E-5

# Doppler method Selection effects

For a given stellar mass, the amplitude of the reflex motion scales as  $M_p P^{-1/3}$ Easier to detect massive planets with short orbital periods (i.e., small semimajor axis)

For a given planetary mass, the amplitude of the reflex motion scales as  $M_*^{-2/3}$  Easier to detect planets around low-mass stars (e.g. M type stars)

Low-mass stars are intrinsically fainter, but more numerous, than stars of higher mass

The amplitude of the reflex motion is larger when the line of sight is aligned with the orbital plane ( $\sin i \cong 1$ )

This bias favours the detection of planetary orbits coplanar with the line of sight. This bias does not affect the measurement of physical properties.

- Derivation of orbital and planetary parameters with the Doppler method
  - The radial velocity curves provides the period, P, from which the semimajor axis a is inferred using the third Kepler's law
  - The mass of the star is derived from a spectroscopic study combined with a model of stellar structure
  - By fitting the radial velocity curve one can obtain the eccentricity, e, and the argument of the pericenter,  $\omega$
  - In this way, from the semiamplitude K one derives the minimum mass, i.e. a lower limit on the planetary mass

$$M_p \sin i = K \left(\frac{P}{2\pi G}\right)^{1/3} (M_\star + M_p)^{2/3} (1 - e^2)^{1/2}$$

#### The orbital inclination

- Systems with high inclination give a higher radial radial velocity signal and, in this sense, are more likely to be detected
- Statistically, the correction term  $\sin i$  is not very large
- The statistical probability for the orbital inclination to lie in a given range  $(i_1, i_2)$  is (Fischer et al. 2014)

$$\mathcal{P} = |\cos(i_2) - \cos(i_1)|$$

- There is roughly an 87% probability that random orbital inclinations are between 30 and 90, or equivalently, an 87% probability that the true mass is within a factor of 2 of the minimum mass  $M_p \sin i$
- In any case, a safe determination of the mass requires an independent measurement of the orbital inclination, i

#### Doppler method

### Cross correlation spectroscopy

Information on the instantaneous Doppler shift is contained in the many thousands of absorption lines present in the high-resolution optical spectra of solar-type stars

This information can be concentrated into a few parameters by cross-correlation with a template of the expected stellar spectrum

In practice, one determines the velocity shift  $\epsilon$ by minimizing the quantity

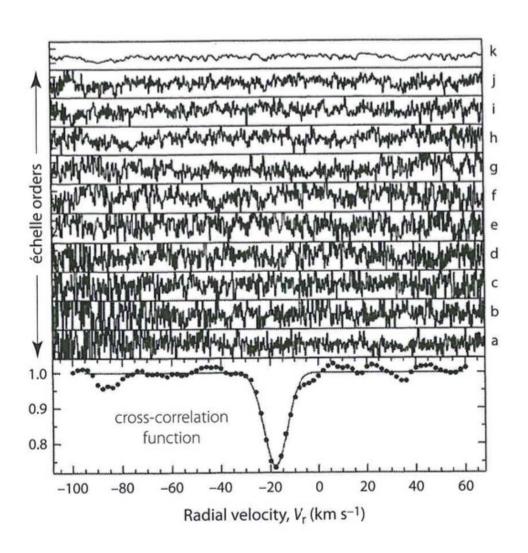
$$C(\epsilon) = \int_{-\infty}^{+\infty} S(v) M(v - \epsilon) dv$$

where S is the spectrum, M is the mask (i.e. a numerical template), both expressed in velocity space v

Thanks to the use of thousands of absorption lines, the cross correlation technique is efficient even at low signal-to-noise ratios

# Doppler method Cross correlation spectroscopy

Example of cross-correlation function for a K0 III star with S/N ~ 1. Observations at R=40000 in 10 echelle orders, each covering ~ 4 nm. About 1000 lines match the template. The resulting cross-correlation function is shown at the bottom. (Queloz 1995)



### Doppler method

### Technological requirements

Extremely stable spectrograph

- Long term stability in temperature (possibly years)
- The spectrograph is closed in a separate room/container, fed by optical fibres

High accuracy of wavelength calibration

- Control of the optical paths of the stellar and wavelength calibration spectra
- Thorium-argon calibration
   Classic observations
- Laser frequency combs

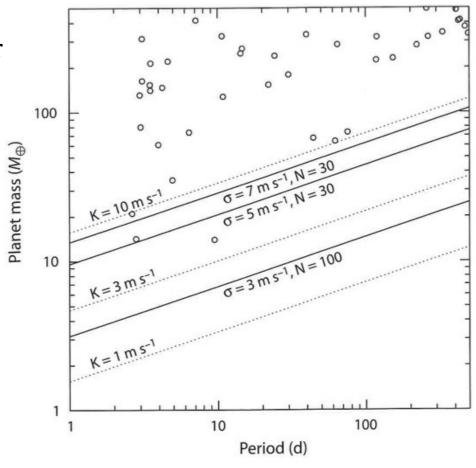
Cover the entire wavelength range of interest with a series of calibration lines of uniform spacing and intensity and accurately known wavelengths determined by fundamental physics

#### Mass limit of detectability

Minimum mass limit (50% detection threshold) as a function of the number of observations, N, and the combined error,  $\sigma$ , for  $M_*=1$  M<sub>sun</sub>

In addition to the measurement error, also the "stellar jitter" (activity in the stellar atmosphere and stellar oscillations) contributes to the combined error  $\sigma$ 

With increasing measurement accuracy, stellar jitter becomes the most severe limit of application of the method



# Doppler method: examples of spectrographs

#### HARPS

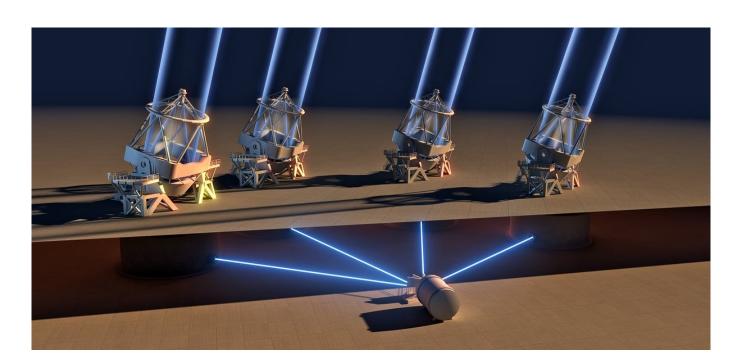
- High Accuracy Radial velocity Planet Searcher
- Telescope: ESO 3.6m La Silla (Cile)
  - http://www.eso.org/sci/facilities/lasilla/instruments/harps/
- Has played a pioneering role, and is still effective, in the search for extrasolar planets
- Estremely stable, with current limits of radial velocity accuracy ~40 cm/s for planets orbiting relatively bright stars (V~12)

#### HARPS-north

- Based on the HARPS spectrograph, installed in 2012 at the Italian national telescope TNG (3.5m, La Palma, Spain)
- Extends the capabilities of HARPS to the northern hemisphere

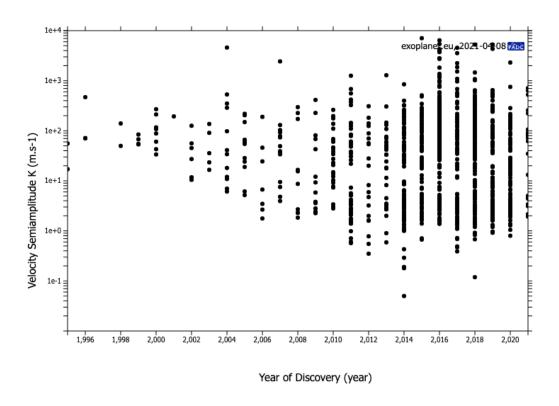
#### ESPRESSO

- Echelle SPectrograph for Rocky Exoplanet and Stable Spectroscopic Observations
  - http://www.eso.org/sci/facilities/develop/instruments/espresso.html
- Extremely stable, recently installed at the combined focus of the ESO VLT (8m x 4)
  - Radial velocity accuracy: < 10 cm/s
  - Fainter stars than observable with HARPS
- Detection of terrestrial-type planets at  $\sim$ 1 AU around solar-type stars



### Doppler method

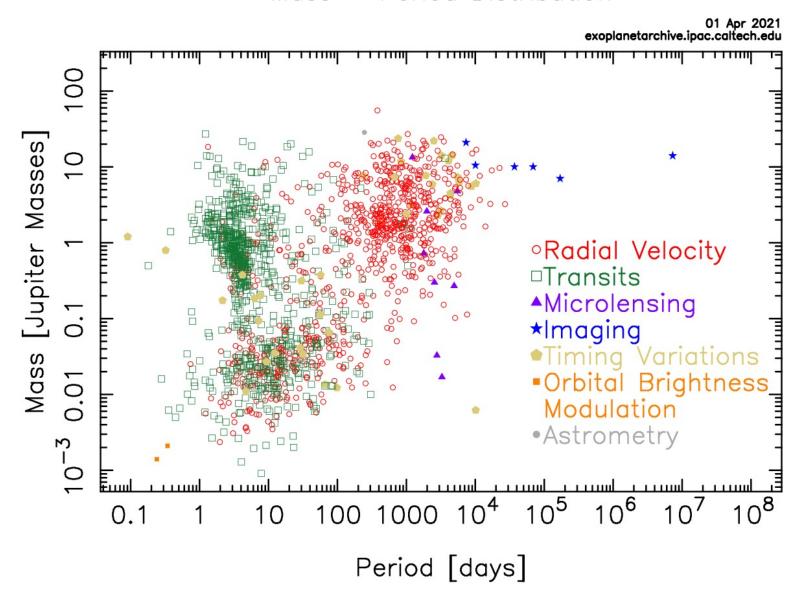
- Between 1995 and 2012 most exoplanets have been discovered with the Doppler method
- Currently (April 2021) detected 914 planets in 678 planetary systems



## Radial velocity method

#### Comparison with other methods

Mass - Period Distribution



# Detection of <u>multiple planetary systems</u> with the Doppler method

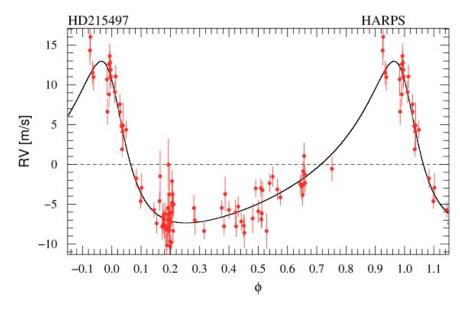
• The total radial velocity signal due an orbiting system of  $n_p$  planets is assumed to result from the independent reflex motions due to each planet separately

#### • Procedure:

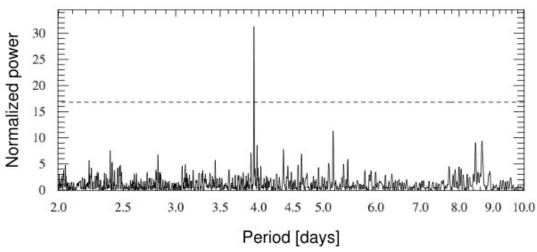
- Make a Keplerian fit of the most intense signal of the radial velocity curve
- Subract the Keplerian fit to the experimental data and search for more periodic signals in the residuals
- If the periodogram (Fourier transform) of the residuals shows a peak above the noise level, a further Keplerian fit is performed
- The procedure can be iterated if the periodogram of the residuals shows additional significant peaks

Example: Two-planet system orbiting HD215497 (Lo Curto et al. 2010)

Detection of the planet that yields the main signal (P= 568 d)



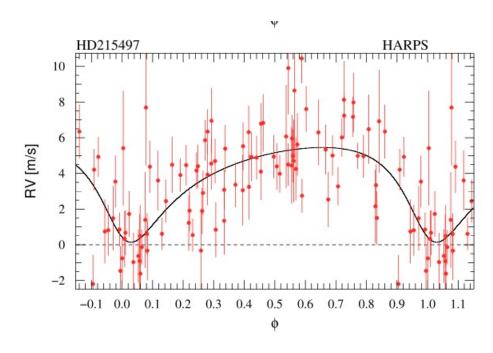
The periodogram of the residuals shows a peak at *P*=3.93 d, well above the noise level



# Example: Two-planet system orbiting HD215497 (Lo Curto et al. 2010)

Keplerian fit of the residuals, using the orbital parameters determined from the previous step

Final results



Parameter	HD 215497b	HD 215497c	
P [days]	$3.93404 \pm 0.00066$	$567.94 \pm 2.70$	
T [JD-2 400 000]	$54858.95 \pm 0.37$	$55003.48 \pm 5.15$	
e	$0.16 \pm 0.09$	$0.49 \pm 0.04$	
$\omega$ [deg]	$96 \pm 34$	$45 \pm 4$	
$K [m s^{-1}]$	$2.98 \pm 0.34$	$10.10 \pm 0.65$	
$V [\mathrm{km} \; \mathrm{s}^{-1}]$	$49.3107 \pm 0.0006$		
$m \sin i [M_{Jup}]$	0.02	0.33	
$m \sin i [M_{\text{Earth}}]$	6.6	104.3	
a [AU]	0.047	1.282	
**	405		

# Doppler method future projects

#### CODEX

- Instrument concept for the European ELT (Extremely Large Telescope)
- It aims to detect the expansion of the Universe directly, by measuring the Doppler shift of high-redshift quasar Ly-α absorption lines as a function of time
- The experiment targets a Doppler accuracy of ~0.02 m/s mantained over several <u>decades</u>
- The design has developed from HARPS and will incorporate all the state-of-the-art technology (e.g. laser comb, etc.)
- CODEX will have direct application to exoplanet studies
- Stellar jitter would definitely become the major limitation